

- g) E^{-1} equal to
 (A) $1-\nabla$ (B) $1+\nabla$ (C) $1+\delta$ (D) $1-\delta$
- h) hD equal to
 (A) $\log(1+\Delta)$ (B) $\log(1-\Delta)$ (C) $\log(1+E)$ (D) $\log(1-E)$
- i) The n th difference of a polynomial of degree n is
 (A) constant (B) zero (C) $n!$ (D) none of these
- j) In application of Simpson's $\frac{1}{3}$ rule, the interval of integration for closer approximation should be
 (A) odd and small (B) even and small (C) even and large (D) none of these
- k) The convergence in the Gauss – Seidel method is faster than Gauss – Jacobi method.
 (A) TRUE (B) FALSE
- l) The Gauss – Jordan method in which the set of equations are transformed into diagonal matrix form.
 (A) TRUE (B) FALSE
- m) Using modified Euler's method, the value of $y(0.1)$ for $\frac{dy}{dx} = x - y$, $y(0) = 1$ is
 (A) 0.909 (B) 0.809 (C) 0.0809 (D) 0.0908
- n) Which of the following methods is the best for solving initial value problems:
 (A) Taylor's series method (B) Euler's method
 (C) Runge-Kutta method of 4th order (D) Modified Euler's method

Attempt any four questions from Q-2 to Q-8

Q-2 Attempt all questions (14)

- a) Use Stirling's formula to find y_{28} given that $y_{20} = 49225$, $y_{25} = 48316$, $y_{30} = 47236$, $y_{35} = 45926$ and $y_{40} = 44306$. (5)
- b) Construct Newton's forward interpolation polynomial to the following data: (5)

x	4	6	8	10
y	1	3	8	16

- c) Find the Fourier sine transform of $f(x) = \begin{cases} 0 & 0 < x < a \\ x & a \leq x \leq b \\ 0 & x > b \end{cases}$ (4)

Q-3 Attempt all questions (14)

- a) Solve the following system of equations by Gauss-Seidal method. (5)
 $10x_1 + x_2 + 2x_3 = 44$, $2x_1 + 10x_2 + x_3 = 51$, $x_1 + 2x_2 + 10x_3 = 61$
- b) The population of a certain town is shown in the following table: (5)

Year	1961	1971	1981	1991	2001
Population (in thousands)	19.96	36.65	58.81	77.21	94.61



Find the rate of growth of population in 1991.

- c) Show that $u(x, y) = 2x - x^3 + 3xy^2$ is harmonic in some domain and find a harmonic conjugate of $u(x, y)$. (4)

Q-4 Attempt all questions (14)

- a) Use Euler's method to find an approximate value of y at $x = 0.1$, in five steps, given that $\frac{dy}{dx} = x - y^2$ and $y(0) = 1$. (5)

- b) Evaluate $\int_0^{0.6} e^{-x^2} dx$ by using Simpson's 1/3rd rule. (5)

- c) Solve the following system of equations using Gauss-elimination method: (4)

$$-x_1 + x_2 + 2x_3 = 2, \quad 3x_1 - x_2 + x_3 = 6, \quad -x_1 + 3x_2 + 4x_3 = 4$$

Q-5 Attempt all questions (14)

- a) Show that the function $f(z) = \sqrt{|xy|}$ is not analytic at the origin, although Cauchy-Riemann equations are satisfied. (5)

- b) Using Green's Theorem, evaluate $\oint_C [(y - \sin x)dx + \cos x dy]$ where C is (5)

the plane triangle enclosed by the lines $y = 0$, $x = \frac{\pi}{2}$ and $y = \frac{2}{\pi}x$.

- c) Compute $f(9.2)$ by using Lagrange Interpolation formula from the following data: (4)

x	9	9.5	11
y	2.1972	2.2513	2.3979

Q-6 Attempt all questions (14)

- a) Prove that $\vec{F} = (y^2 \cos x + z^3)\hat{i} + (2y \sin x - 4)\hat{j} + 3xz^2\hat{k}$ is irrotational and find its scalar potential. (5)

- b) Find the bilinear transformation which sends the points $z = 0, 1, \infty$ into the points $w = -5, -1, 3$ respectively. What are the invariant points of the transformation? (5)

- c) Solve $\frac{dy}{dx} = 3 + 2xy$ where $y(0) = 1$ for $x = 0.1$ by Picard's method. (4)

Q-7 Attempt all questions (14)

- a) Using Cauchy - Riemann equations, prove that if $f(z) = u + iv$ is analytic with constant modulus, then u, v are constants. (5)

- b) If $\vec{F} = (2xy + z^3)\hat{i} + x^2\hat{j} + 3xz^3\hat{k}$, show that $\int_C \vec{F} \cdot d\vec{r}$ is independent of the (5)

path of integration. Hence evaluate the integral when C is any path joining $A(1, -2, 1)$ to $B(3, 1, 4)$.

- c) The function $f(x)$ is given as follows: (4)

x	0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9	1.0
y	1	1.2	1.4	1.6	1.8	2.0	2.2	2.4	2.6	2.8	3.0

Compute the integral of $f(x)$ between $x = 0$ and $x = 1.0$ using Trapezoidal rule.



Q-8

Attempt all questions

(14)

- a) Using Taylor's series method, compute $y(-0.1)$, $y(0.1)$, $y(0.2)$ correct to four decimal places, given that $\frac{dy}{dx} = y - \frac{2x}{y}$, $y(0) = 1$ **(5)**
- b) Find the Fourier cosine and sine integral of $f(x) = e^{-kx}$ ($x > 0$, $k > 0$). **(5)**
- c) Find the angle between the tangents to the curve $x = t^2$, $y = 2t$, $z = -t^3$ at the points $t = 1$ and $t = -1$. **(4)**

